

High Speed Camera & IMUs on Mobile Devices

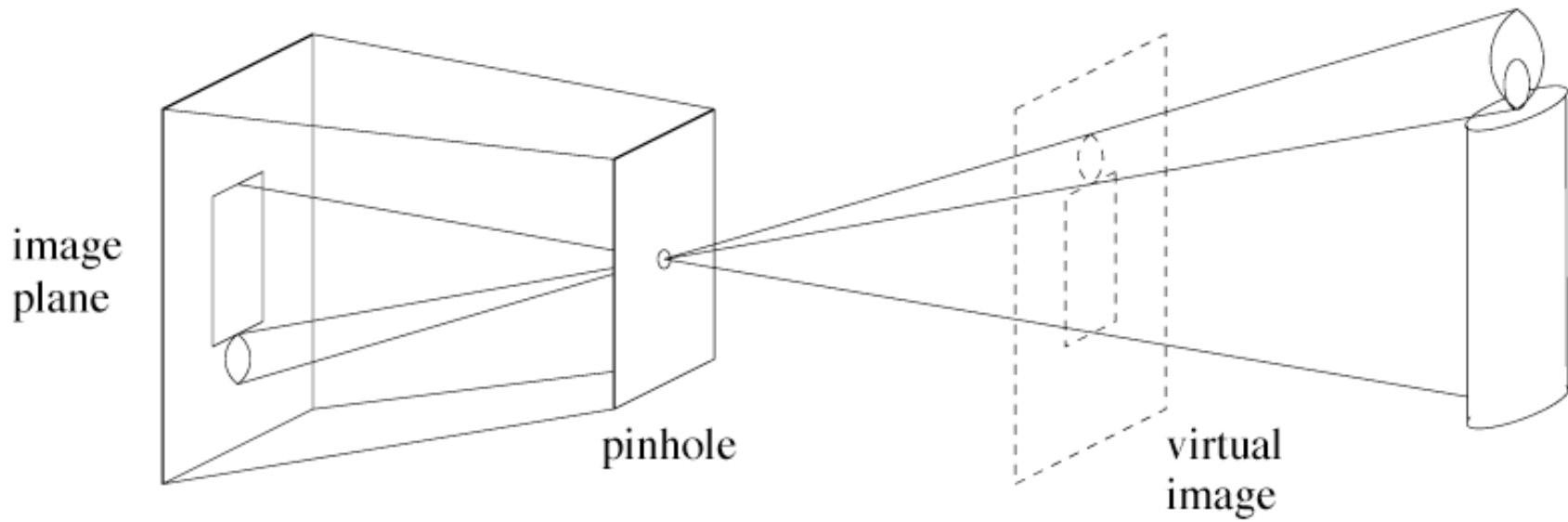
Instructor - Simon Lucey

16-623 - Designing Computer Vision Apps

Today

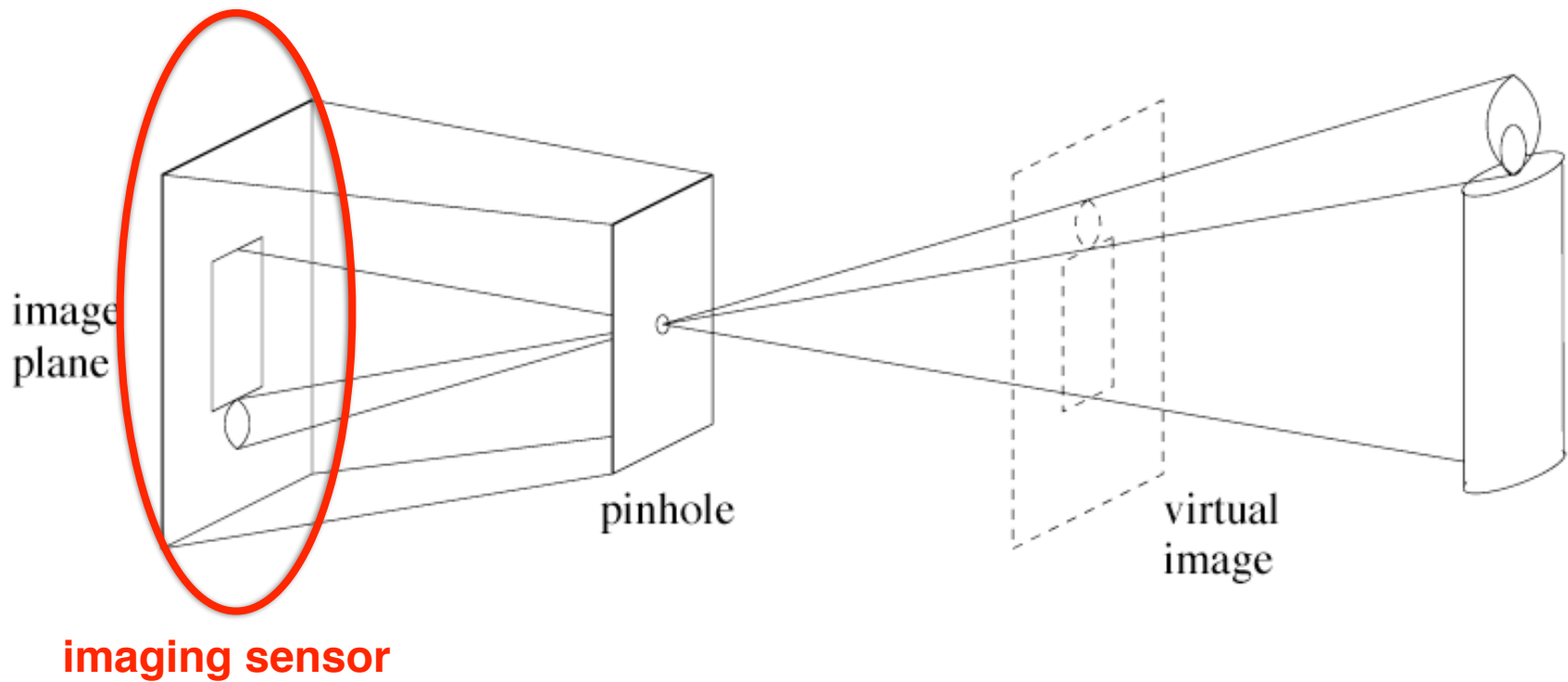
- CCD vs CMOS cameras.
- Rolling Shutter Epipolar Geometry
- Inertial Measurement Units (IMU)

Pinhole Camera



(Taken from Forsyth & Ponce)

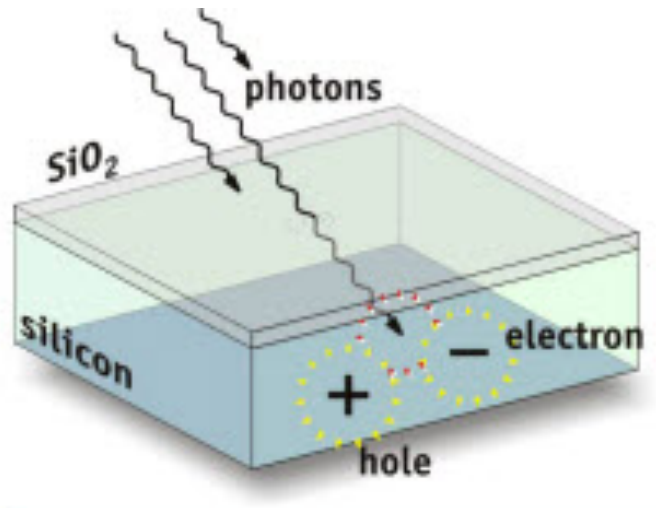
Pinhole Camera



(Taken from Forsyth & Ponce)

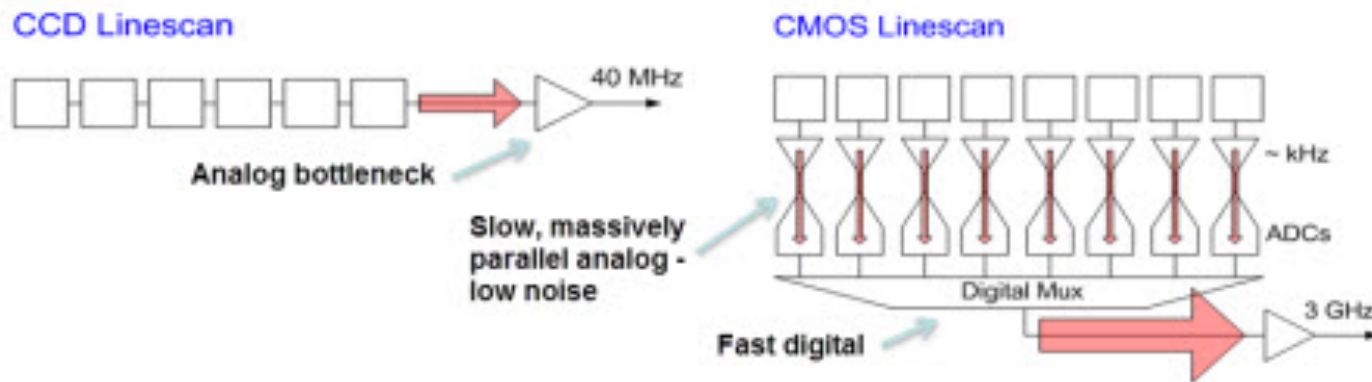
Digital Cameras

- All digital cameras rely on the photoelectric effect to create electrical signal from light.
- CCD (charge coupled device) and CMOS (complementary metal oxide semiconductor) are the two most common image sensors found in digital cameras.
- Both invented in the late 60s early 70s.



CCD versus CMOS

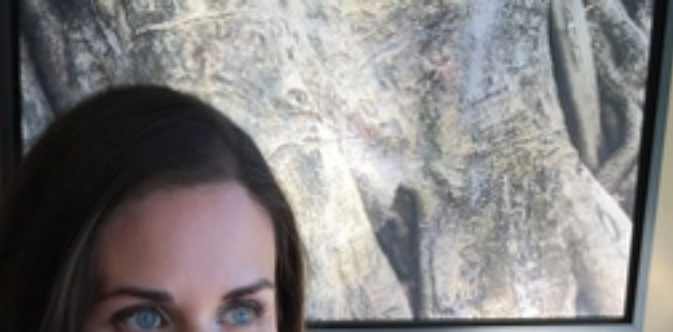
- CMOS and CCD imagers differ in the way that signals are converted from signal charge.

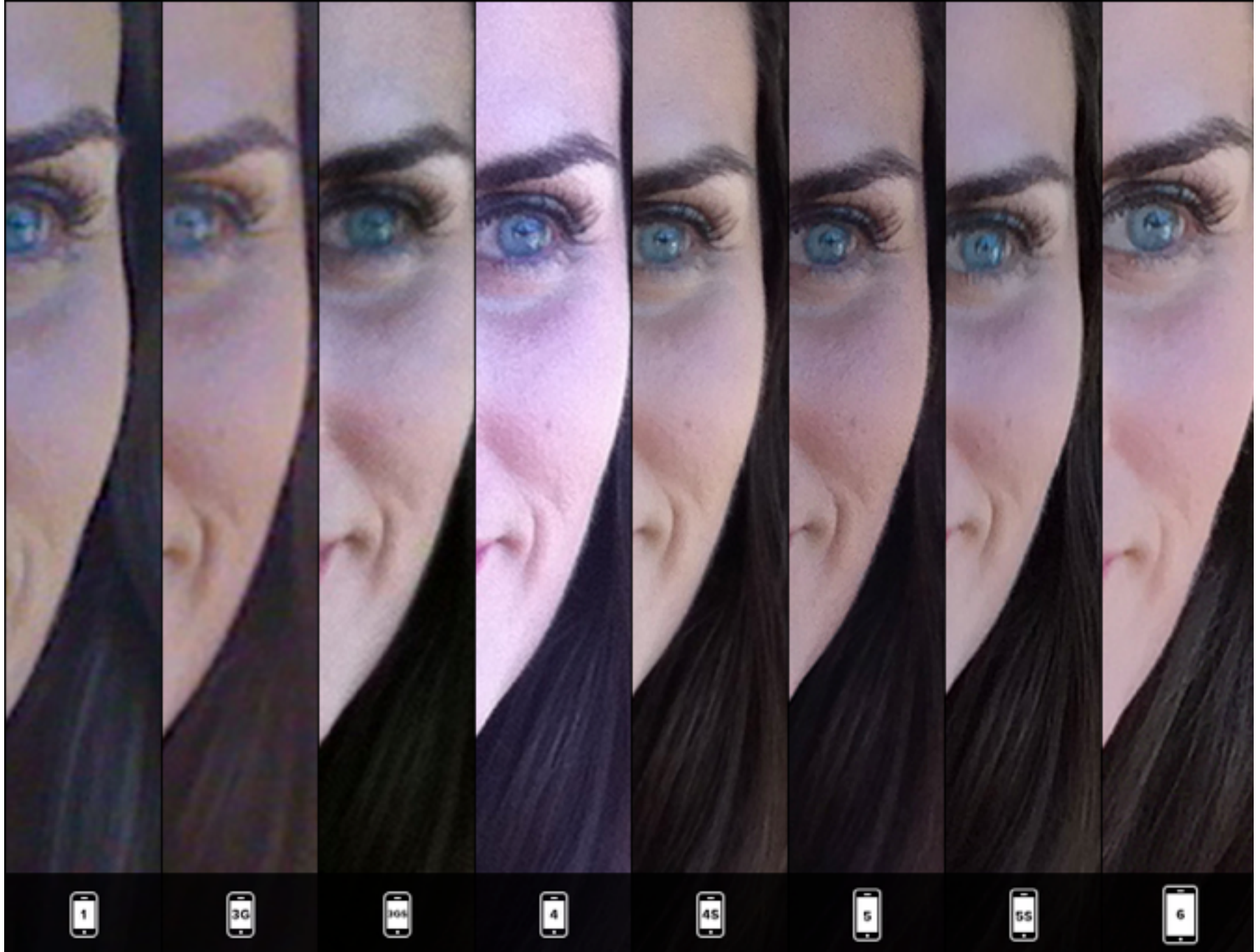


- CMOS imagers are inherently more parallel than CCDs.
- Consequently, high speed CMOS imagers can be designed to have much lower noise than high speed CCDs.

CCD versus CMOS

- CCD used to be the image sensor of choice as it gave far superior images with the fabrication technology available.
- CMOS was of interest with the the advent of mobile phones.
 - CMOS promised lower power consumption.
 - lowered fabrication costs (reuse mainstream logic and memory device fabrication).
- An enormous amount of investment was made to develop and fine tune CMOS imagers.
- As a result we witnessed great improvements in image quality, even as pixel sizes shrank.
- In the case of high volume consumer area imagers, CMOS imagers outperform CCDs based on almost every performance parameter.

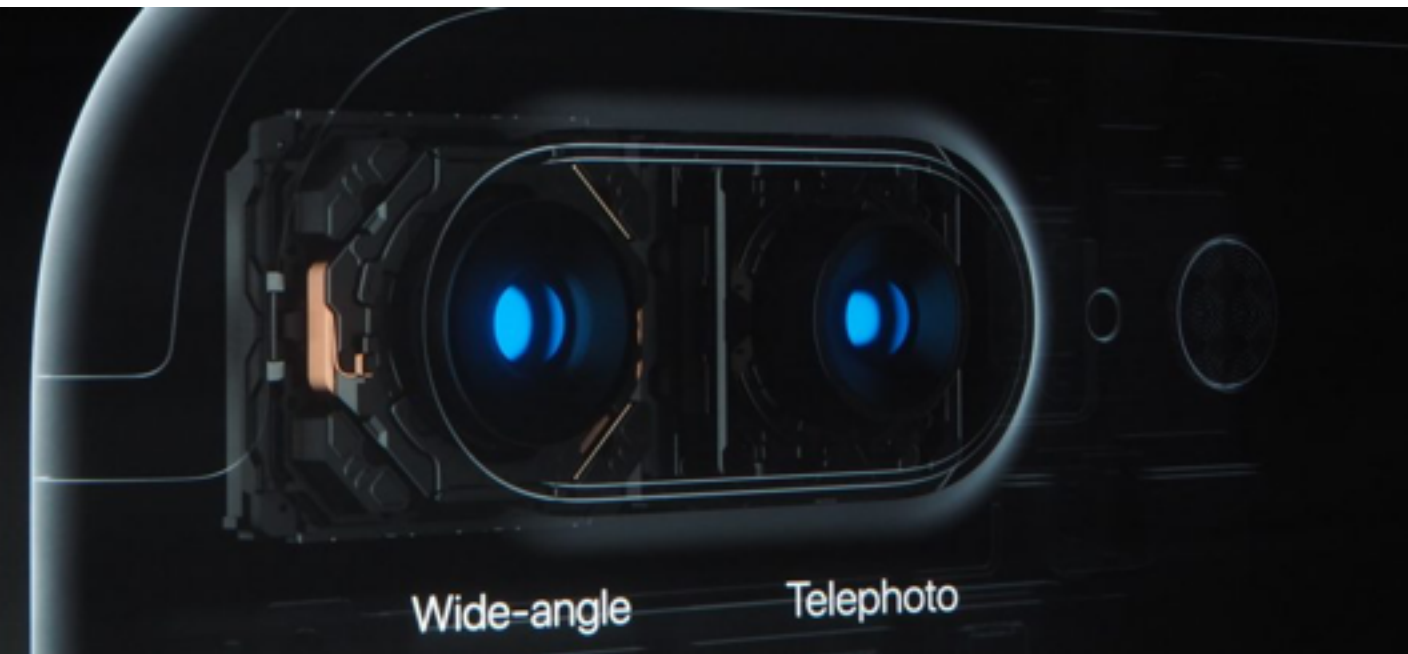




Taken from: <http://9to5mac.com/2014/09/23/iphone-6-camera-compared-to-all-previous-iphones-gallery/>

New Developments - iPhone 7

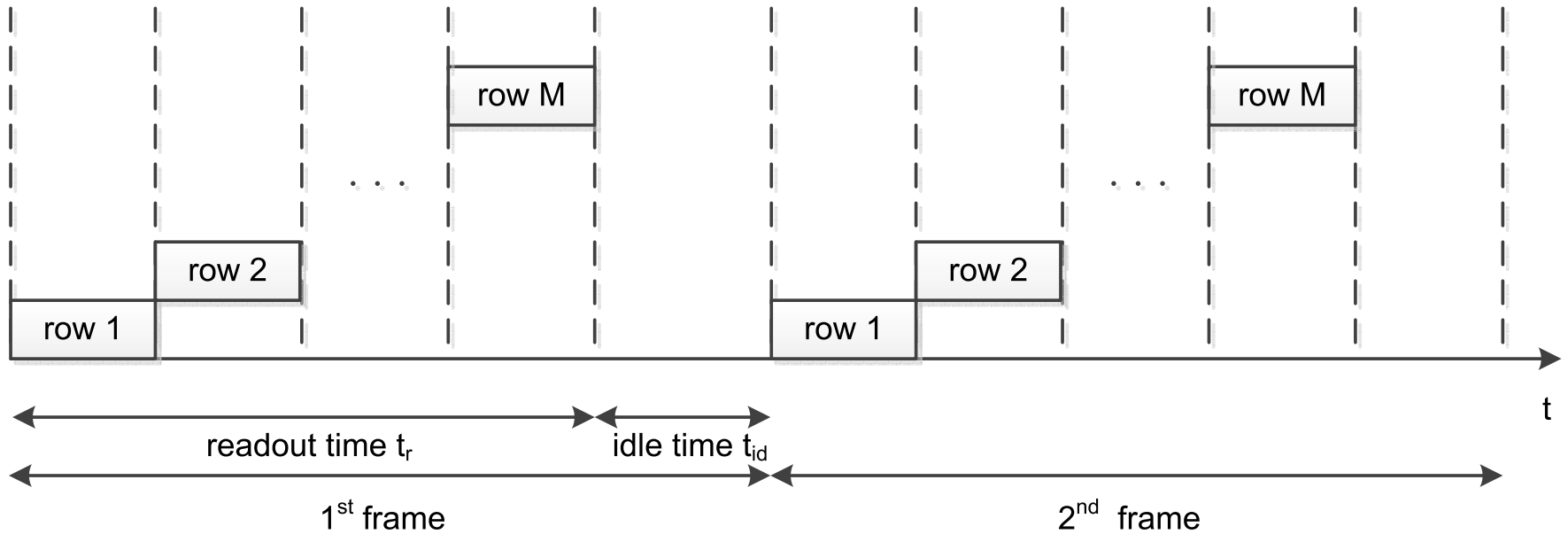
- Apple just released the iPhone 7 with new dual lens camera.
- Rumored that advances in the camera are based on the 2015 acquisition of [Linx](#) (Israeli startup).
- Image quality “closest” attempt yet to DSLR on mobile device.



Today

- CCD vs CMOS cameras.
- Rolling Shutter Epipolar Geometry
- Inertial Measurement Units (IMU)

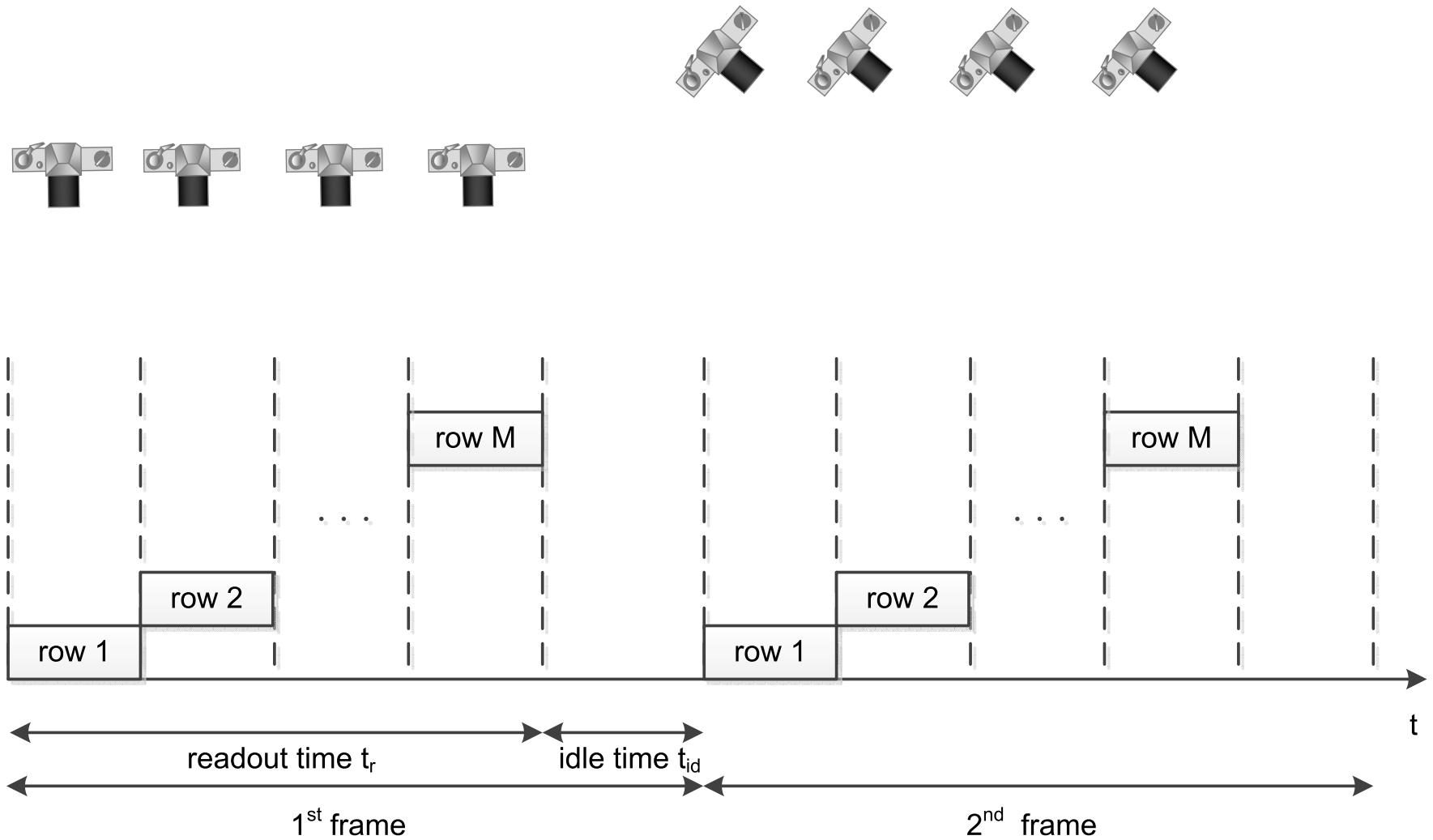
Rolling Shutter Effect



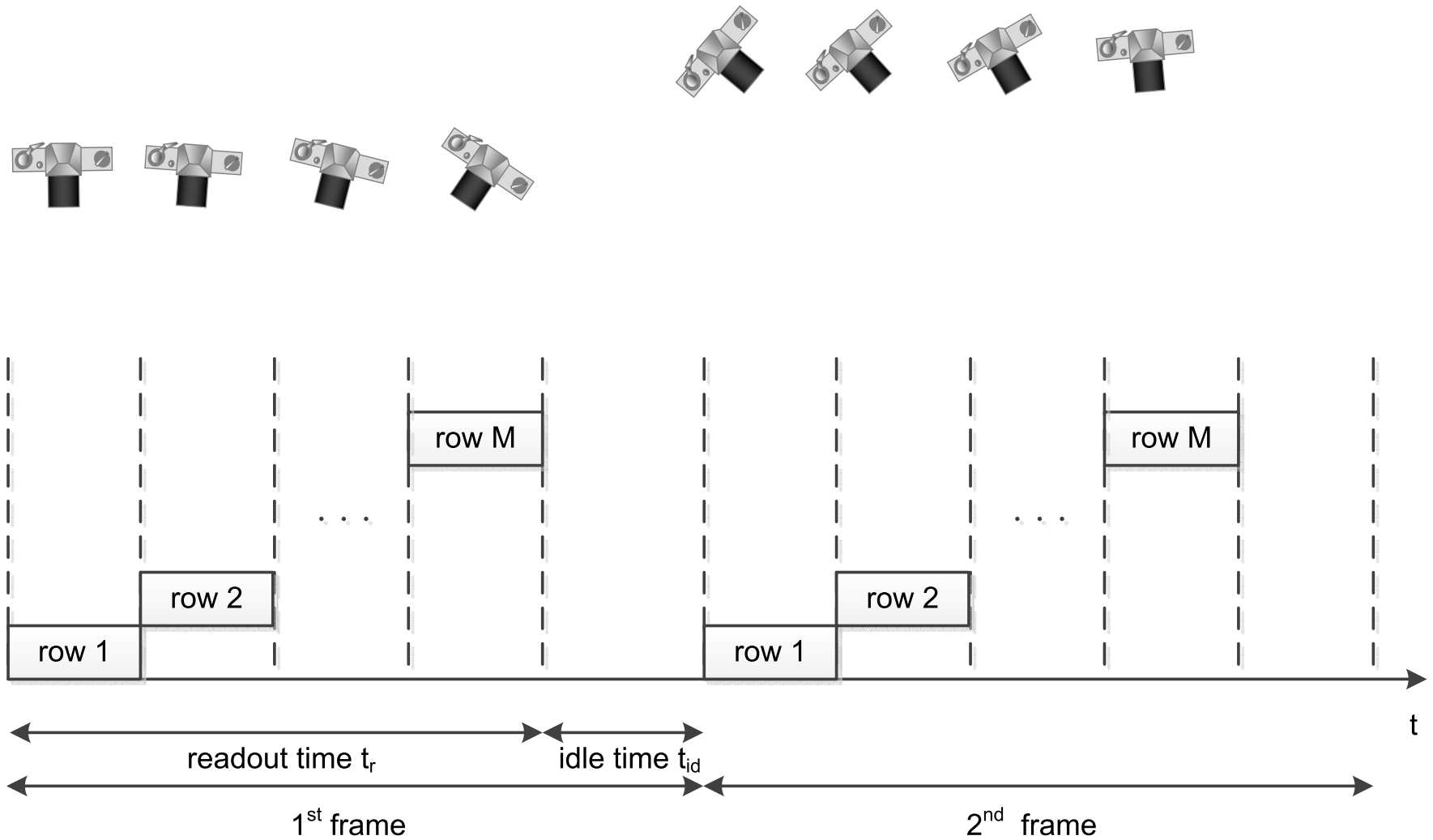
Rolling shutter cameras sequentially expose rows.

$$t_r + t_{id} = \frac{1}{\text{frames per second}}$$

Global versus Rolling Shutter



Global versus Rolling Shutter



Rolling-Shutter Effect



- A drawback to CMOS sensors is the “rolling-shutter effect”.
- CMOS captures images by scanning one line of the frame at a time.
- If anything is moving fast, then it will lead to weird distortions in still photos, and to rather odd effects in video.
- Check out the following video taken with the iPhone 4 CCD camera.
- CCD-based cameras often use a “global” shutter to circumvent this problem.

Rolling-Shutter Effect



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Rolling Shutter Effect = “Aliasing”

- Rolling Shutter Effect is an example of a broader phenomena regularly studied in Signal Processing called “Aliasing”.
- Common phenomenon
 - Wagon wheels rolling the wrong way in movies.



Rolling Shutter Effect = “Aliasing”

- Rolling Shutter Effect is an example of a broader phenomena regularly studied in Signal Processing called “Aliasing”.
- Common phenomenon
 - Wagon wheels rolling the wrong way in movies.



Rectifying Rolling Shutter

- What do you think the camera motion was here?



Taken from: [Hanning et al. "Stabilizing Cell Phone Video using Inertial Measurement Sensors" in ICCV 2011 Workshop.](#)

High-Frame Rate Cameras



- Another way around this is to create higher-frame rate cameras.
- Increasingly seeing faster and faster CMOS cameras.
- Opening up other exciting opportunities in computer vision.
- However, really fast motions still need an understanding of the rolling shutter effect.

High-Frame Rate Cameras

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Rectifying Rolling Shutter

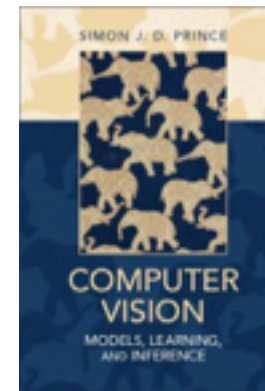
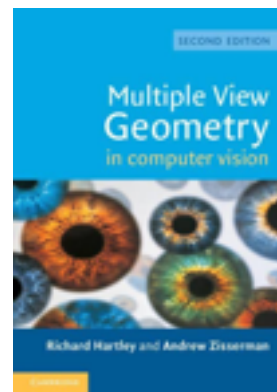
- Result from rectification,



Taken from: [Hanning et al. "Stabilizing Cell Phone Video using Inertial Measurement Sensors" in ICCV 2011 Workshop.](#)

Reminder: Cheat Sheet

Description	Hartley & Zisserman	Prince
3D Point	X	W
2D Point	x	x
Rotation matrix	R	Ω
Intrinsics matrix	K	Λ
Homography matrix	H	Φ
translation vector	t	τ



Reminder: The Essential Matrix

First camera: $\lambda_1 \tilde{\mathbf{x}}_1 = \mathbf{w}$

Second camera:

$$\lambda_2 \tilde{\mathbf{x}}_2 = \Omega \mathbf{w} + \tau$$

Substituting:

$$\lambda_2 \tilde{\mathbf{x}}_2 = \lambda_1 \Omega \tilde{\mathbf{x}}_1 + \tau$$

This is a mathematical relationship between the points in the two images, but it's not in the most convenient form.

Reminder: The Essential Matrix

$$\lambda_2 \tilde{\mathbf{x}}_2 = \lambda_1 \mathbf{\Omega} \tilde{\mathbf{x}}_1 + \boldsymbol{\tau}$$

$$\lambda_2 \boldsymbol{\tau} \times \tilde{\mathbf{x}}_2 = \lambda_1 \boldsymbol{\tau} \times \mathbf{\Omega} \tilde{\mathbf{x}}_1$$

$$\tilde{\mathbf{x}}_2^T \boldsymbol{\tau} \times \mathbf{\Omega} \tilde{\mathbf{x}}_1 = 0$$

Reminder: The Essential Matrix

$$\tilde{\mathbf{x}}_2^T \boldsymbol{\tau} \times \boldsymbol{\Omega} \tilde{\mathbf{x}}_1 = 0$$

The cross product term can be expressed as a matrix

$$\boldsymbol{\tau}_\times = \begin{bmatrix} 0 & -\tau_z & \tau_y \\ \tau_z & 0 & -\tau_x \\ -\tau_y & \tau_x & 0 \end{bmatrix}$$

Defining:

$$\mathbf{E} = \boldsymbol{\tau}_\times \boldsymbol{\Omega}$$

We now have the essential matrix relation

$$\tilde{\mathbf{x}}_2^T \mathbf{E} \tilde{\mathbf{x}}_1 = 0$$

Epipolar Geometry for Rolling Shutter

- Recently Dai et al. (2016) developed Generalized Epipolar Geometry for Rolling Shutter Camera.
- Assuming linear rolling shutter,

$$\lambda_1 \tilde{\mathbf{x}}_1 = \mathbf{w} + \nu_1 \mathbf{d}_1$$

$$\lambda_2 \tilde{\mathbf{x}}_2 = \Omega \mathbf{w} + \boldsymbol{\tau} + \nu_2 \mathbf{d}_2$$

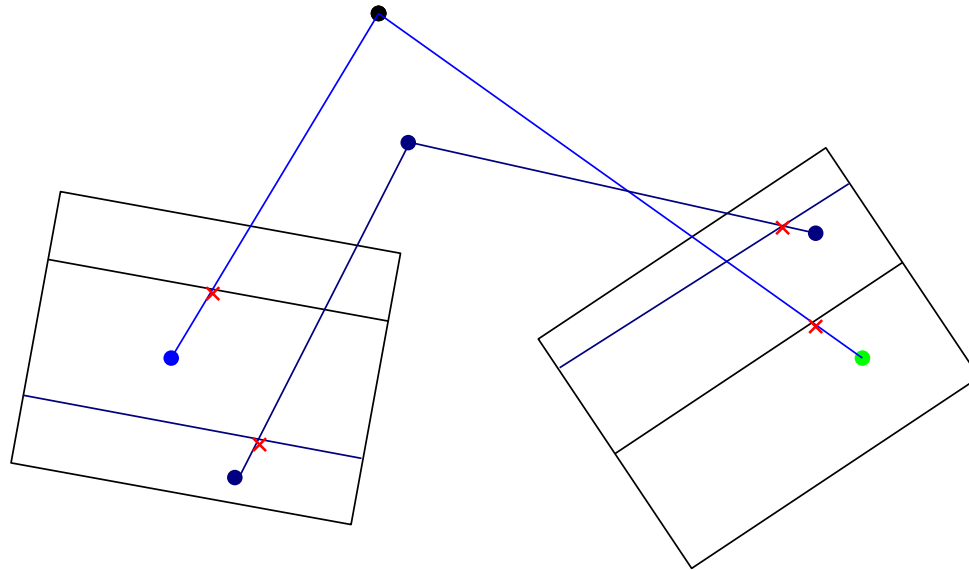
$\nu \rightarrow$ index to the scan line in the image

$\mathbf{d}_i \rightarrow$ 3D velocity for *i-th* viewpoint

Epipolar Geometry for Rolling Shutter

- Results in a different essential matrix for every possible combination of ν_1 and ν_2 .

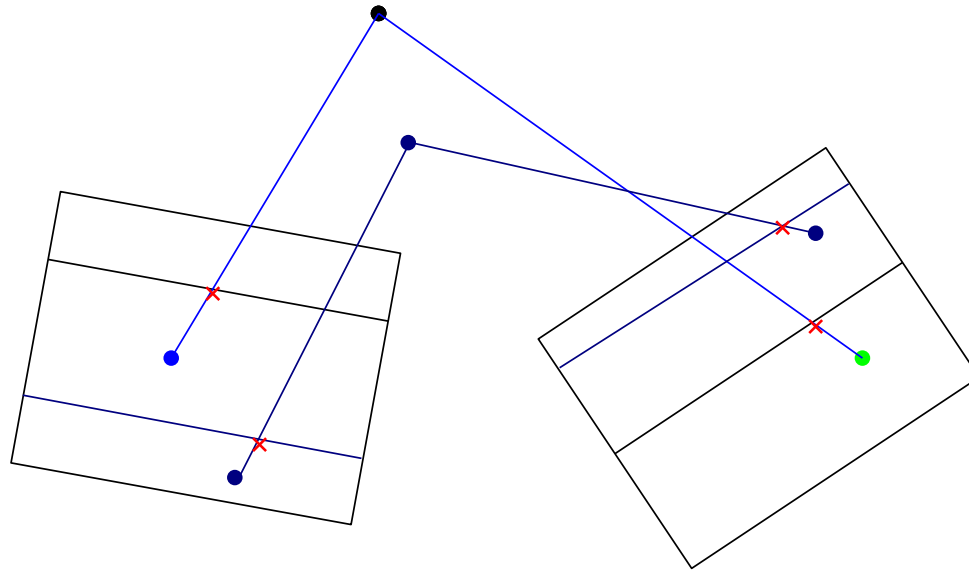
$$\mathbf{E}(\nu_1, \nu_2) = (\boldsymbol{\tau} + \nu_2 \mathbf{d}_2 - \nu_1 \boldsymbol{\Omega} \mathbf{d}_1) \times \boldsymbol{\Omega}$$



Epipolar Geometry for Rolling Shutter

- Results in a different essential matrix for every possible combination of ν_1 and ν_2 .

$$\mathbf{E}(\nu_1, \nu_2) = (\boldsymbol{\tau} + \nu_2 \mathbf{d}_2 - \nu_1 \boldsymbol{\Omega} \mathbf{d}_1) \times \boldsymbol{\Omega}$$



How many degrees of freedom?

Epipolar Geometry for Rolling Shutter

Camera Model	Essential Matrix	Monomials	Degree-of-freedom	Linear Algorithm	Non-linear Algorithm	Motion Parameters
Perspective camera	$\begin{bmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{bmatrix}$	$(u_i, v_i, 1)$	$3^2 = 9$	8-point	5-point	\mathbf{R}, \mathbf{t}
Linear push broom	$\begin{bmatrix} 0 & 0 & f_{13} & f_{14} \\ 0 & 0 & f_{23} & f_{24} \\ f_{31} & f_{32} & f_{33} & f_{34} \\ f_{41} & f_{42} & f_{43} & f_{44} \end{bmatrix}$	$(u_i v_i, u_i, v_i, 1)$	$12 = 4^2 - 2^2$	11-point	11-point	$\mathbf{R}, \mathbf{t}, \mathbf{d}_1, \mathbf{d}_2$
Linear rolling shutter	$\begin{bmatrix} 0 & 0 & f_{13} & f_{14} & f_{15} \\ 0 & 0 & f_{23} & f_{24} & f_{25} \\ f_{31} & f_{32} & f_{33} & f_{34} & f_{35} \\ f_{41} & f_{42} & f_{43} & f_{44} & f_{45} \\ f_{51} & f_{52} & f_{53} & f_{54} & f_{55} \end{bmatrix}$	$(u_i^2, u_i v_i, u_i, v_i, 1)$	$21 = 5^2 - 2^2$	20-point	11-point	$\mathbf{R}, \mathbf{t}, \mathbf{d}_1, \mathbf{d}_2$
Uniform push broom	$\begin{bmatrix} 0 & 0 & f_{13} & f_{14} & f_{15} & f_{16} \\ 0 & 0 & f_{23} & f_{24} & f_{25} & f_{26} \\ f_{31} & f_{32} & f_{33} & f_{34} & f_{35} & f_{36} \\ f_{41} & f_{42} & f_{43} & f_{44} & f_{45} & f_{46} \\ f_{51} & f_{52} & f_{53} & f_{54} & f_{55} & f_{56} \\ f_{61} & f_{62} & f_{63} & f_{64} & f_{65} & f_{66} \end{bmatrix}$	$(u_i^2 v_i, u_i^2, u_i v_i, u_i, v_i, 1)$	$32 = 6^2 - 2^2$	31-point	17-point	$\mathbf{R}, \mathbf{t}, \mathbf{w}_1, \mathbf{w}_2, \mathbf{d}_1, \mathbf{d}_2$
Uniform rolling shutter	$\begin{bmatrix} 0 & 0 & f_{13} & f_{14} & f_{15} & f_{16} & f_{17} \\ 0 & 0 & f_{23} & f_{24} & f_{25} & f_{26} & f_{27} \\ f_{31} & f_{32} & f_{33} & f_{34} & f_{35} & f_{36} & f_{37} \\ f_{41} & f_{42} & f_{43} & f_{44} & f_{45} & f_{46} & f_{47} \\ f_{51} & f_{52} & f_{53} & f_{54} & f_{55} & f_{56} & f_{57} \\ f_{61} & f_{62} & f_{63} & f_{64} & f_{65} & f_{66} & f_{67} \\ f_{71} & f_{72} & f_{73} & f_{74} & f_{75} & f_{76} & f_{77} \end{bmatrix}$	$(u_i^3, u_i^2 v_i, u_i^2, u_i v_i, u_i, v_i, 1)$	$45 = 7^2 - 2^2$	44-point	17-point	$\mathbf{R}, \mathbf{t}, \mathbf{w}_1, \mathbf{w}_2, \mathbf{d}_1, \mathbf{d}_2$

Accessing the Camera in iOS

```
Camera_AvFoundation) Camera_AvFoundation) ViewController.mm) @implementation ViewController

//
// ViewController.m
// Camera_AvFoundation
//
// Created by Simon Lucey on 9/7/16.
// Copyright © 2016 CMU_16623. All rights reserved.
//

#import "ViewController.h"
#include <iostream>

@interface ViewController();
@end

@implementation ViewController

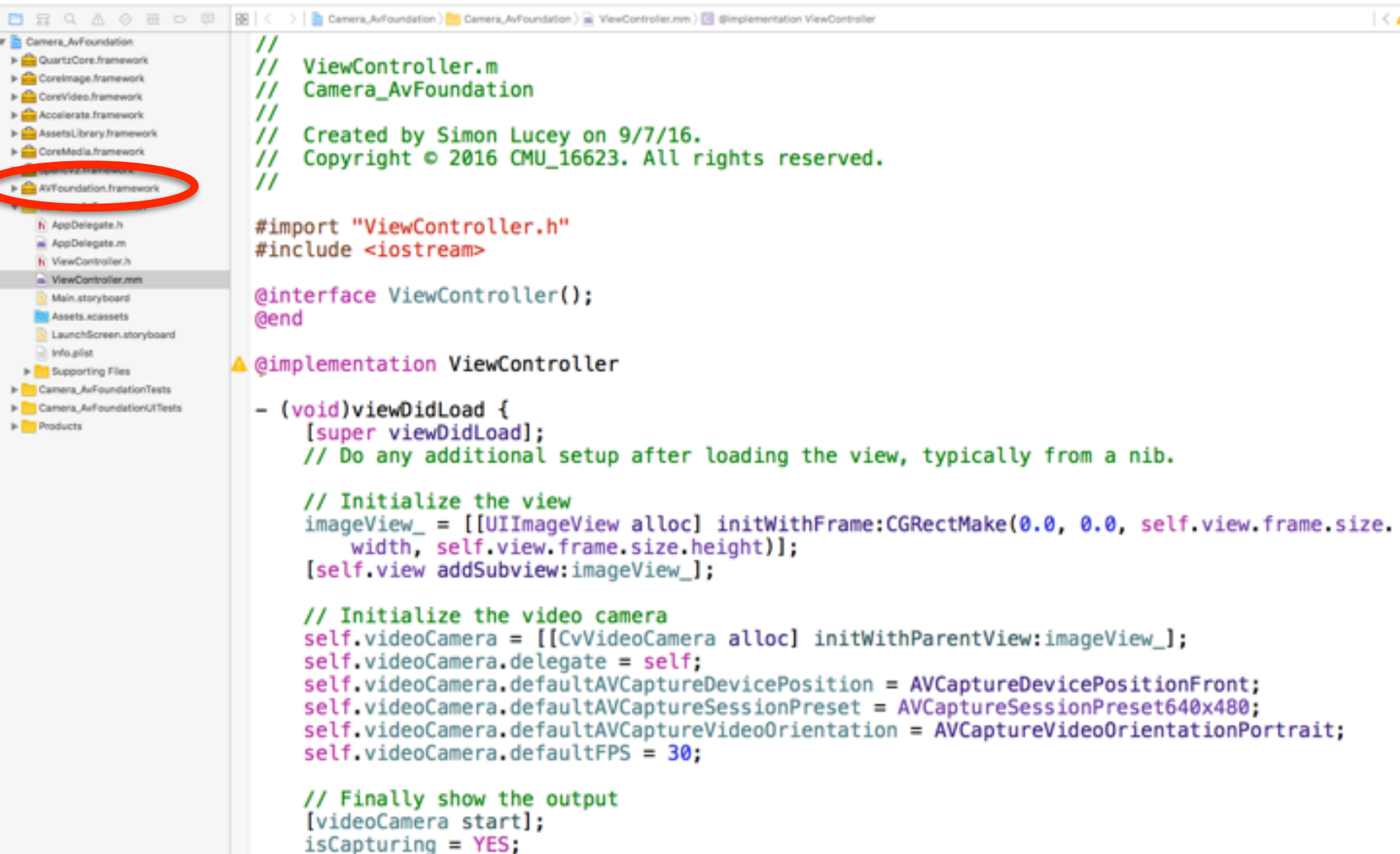
- (void)viewDidLoad {
    [super viewDidLoad];
    // Do any additional setup after loading the view, typically from a nib.

    // Initialize the view
    imageView_ = [[UIImageView alloc] initWithFrame:CGRectMake(0.0, 0.0, self.view.frame.size.
        width, self.view.frame.size.height)];
    [self.view addSubview:imageView_];

    // Initialize the video camera
    self.videoCamera = [[CvVideoCamera alloc] initWithParentView:imageView_];
    self.videoCamera.delegate = self;
    self.videoCamera.defaultAVCaptureDevicePosition = AVCaptureDevicePositionFront;
    self.videoCamera.defaultAVCaptureSessionPreset = AVCaptureSessionPreset640x480;
    self.videoCamera.defaultAVCaptureVideoOrientation = AVCaptureVideoOrientationPortrait;
    self.videoCamera.defaultFPS = 30;

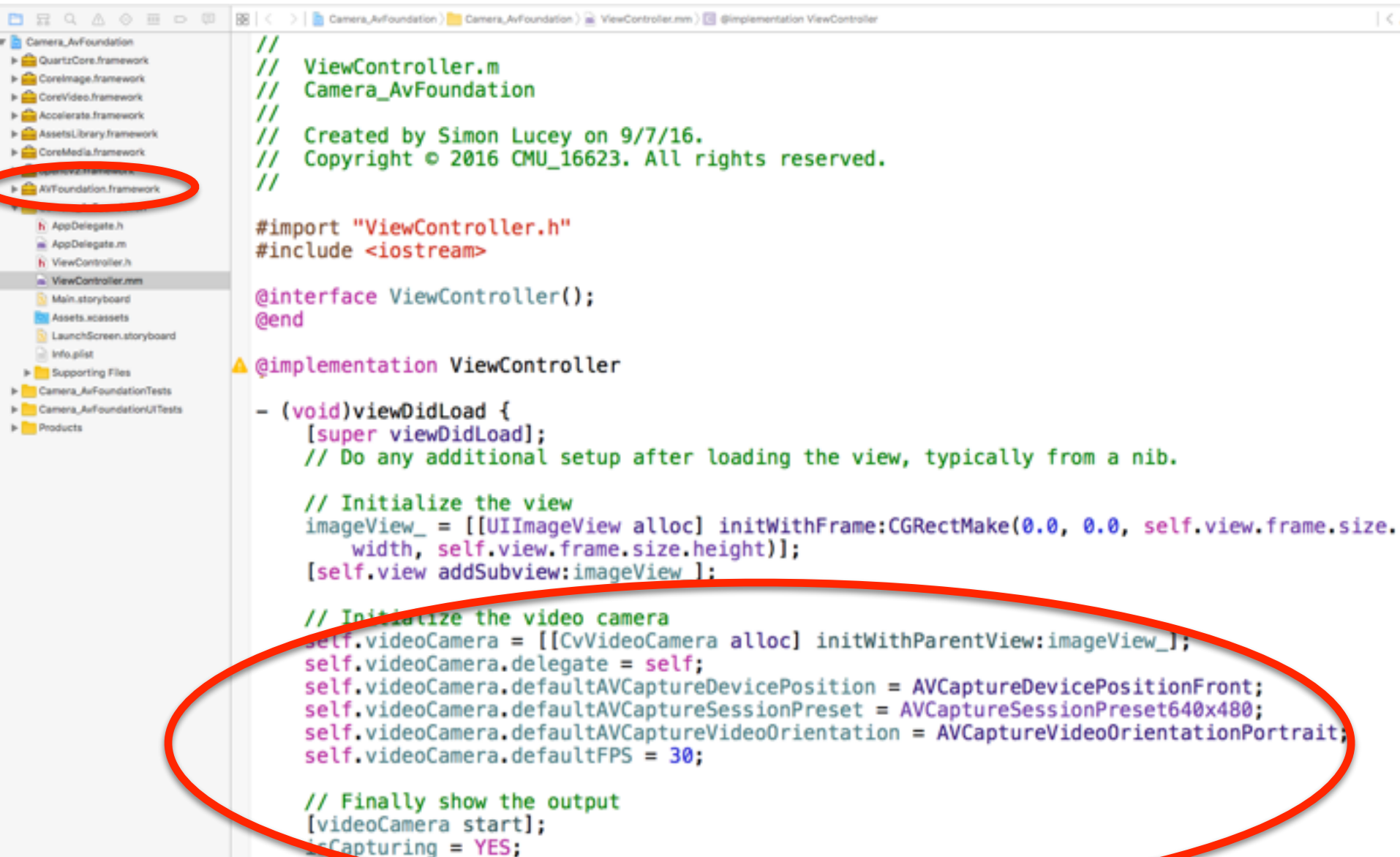
    // Finally show the output
    [videoCamera start];
    isCapturing = YES;
}
```

Accessing the Camera in iOS



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Today

- CCD vs CMOS cameras.
- Rolling Shutter Epipolar Geometry
- Inertial Measurement Units (IMU)

Inertial Measurement Unit

- Measures a device's specific force, angular rate & magnetic field.
- Composed of,
 - Accelerometer.
 - Gyroscope.
 - Magnetometer.
- Historically used heavily within navigation and robotic systems.
- More recently have become common place in smart devices.



Accelerometer



Accelerometer



Accelerometer



What can't you measure?

Gyroscope



IMU Example in iOS

- Good example of using IMU in iOS can be found at,

<https://github.com/nscookbook/recipe19>

- Or better yet, if you have git installed you can type from the command line.

```
$ git clone https://github.com/NSCookbook/recipe19.git
```

- Good tutorial about how code works can be found at,

<http://nscookbook.com/2013/03/ios-programming-recipe-19-using-core-motion-to-access-gyro-and-accelerometer/>

Accessing the IMU in iOS

```
 GyrosAndAccelerometers } GyrosAndAccelerometers } ViewController.m } No Selection
 GyrosAndAccelerometers
 CoreMotion.framework
 GyrosAndAccelerometers
 AppDelegate.h
 AppDelegate.m
 MainStoryboard.storyboard
 ViewController.h
 ViewController.m
 Supporting Files
 Frameworks
 Products

- (void)viewDidLoad
{
    [super viewDidLoad];
    // Do any additional setup after loading the view, typically from a nib.
    currentMaxAccelX = 0;
    currentMaxAccelY = 0;
    currentMaxAccelZ = 0;

    currentMaxRotX = 0;
    currentMaxRotY = 0;
    currentMaxRotZ = 0;

    self.motionManager = [[CMMotionManager alloc] init];
    self.motionManager.accelerometerUpdateInterval = .2;
    self.motionManager.gyroUpdateInterval = .2;

    [self.motionManager startAccelerometerUpdatesToQueue:[NSOperationQueue currentQueue]
                                     withHandler:^(CMAccelerometerData *accelerometerData, NSError *
                                     error) {
        [self outputAccelerationData:accelerometerData.acceleration];
        if(error){
            NSLog(@"%@", error);
        }
    }];

    [self.motionManager startGyroUpdatesToQueue:[NSOperationQueue currentQueue]
                                     withHandler:^(CMGyroData *gyroData, NSError *error) {
        [self outputRotationData:gyroData.rotationRate];
    }];
};
```

Accessing the IMU in iOS



The screenshot shows the Xcode interface. On the left, the project navigator displays the file structure for 'GyroAndAccelerometers', with the 'GyroAndAccelerometers' folder circled in red. The main editor shows the code for 'ViewController.m'.

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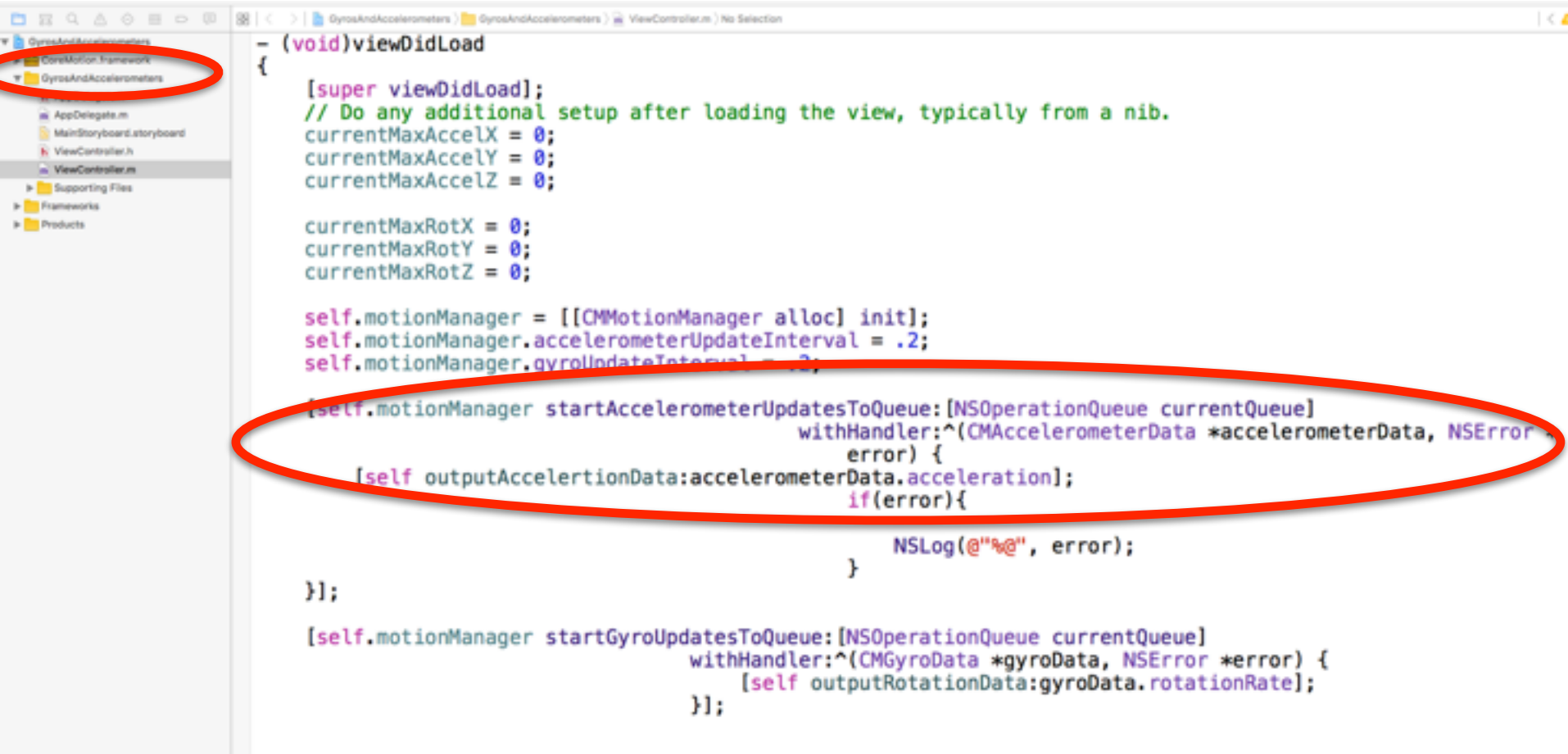
    currentMaxRotX = 0;
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    }];

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Accessing the IMU in iOS



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    }];

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        withHandler:^(CMGyroData *gyroData, NSError *error) {
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    }];
}
```

Accessing the IMU in iOS

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    currentMaxAccelZ = 0;

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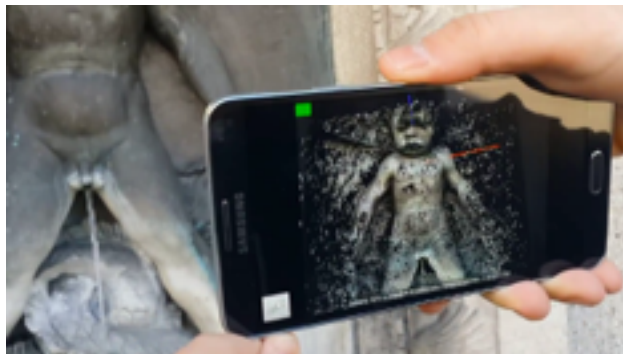
Robotics - Monocular Camera + IMU



- Jones, E., Vedaldi, A., Soatto, S.: Inertial structure from motion with autocalibration. In: Workshop on Dynamical Vision. (2007)
- Weiss, S., Achtelik, M.W., Lynen, S., Achtelik, M.C., Kneip, L., Chli, M., Siegwart, R.: Monocular vision for long-term micro aerial vehicle state estimation: A compendium. Journal of Field Robotics 30(5) (2013) 803–831
- Nutzi, G., Weiss, S., Scaramuzza, D., Siegwart, R.: Fusion of IMU and vision for absolute scale estimation in monocular slam. Journal of Intelligent & Robotic Systems 61(1-4) (2011) 287–299
- Li, M., Kim, B.H., Mourikis, A.I.: Real-time motion tracking on a cellphone using inertial sensing and a rolling-shutter camera. In: IEEE International Conference on Robotics and Automation (ICRA). (2013) 4712–4719

Mobile Solutions

- Tanskanen et al. - ETH Zurich
- Generates accurate point-cloud using SLAM (PTAM)
- Integrates IMU for scale



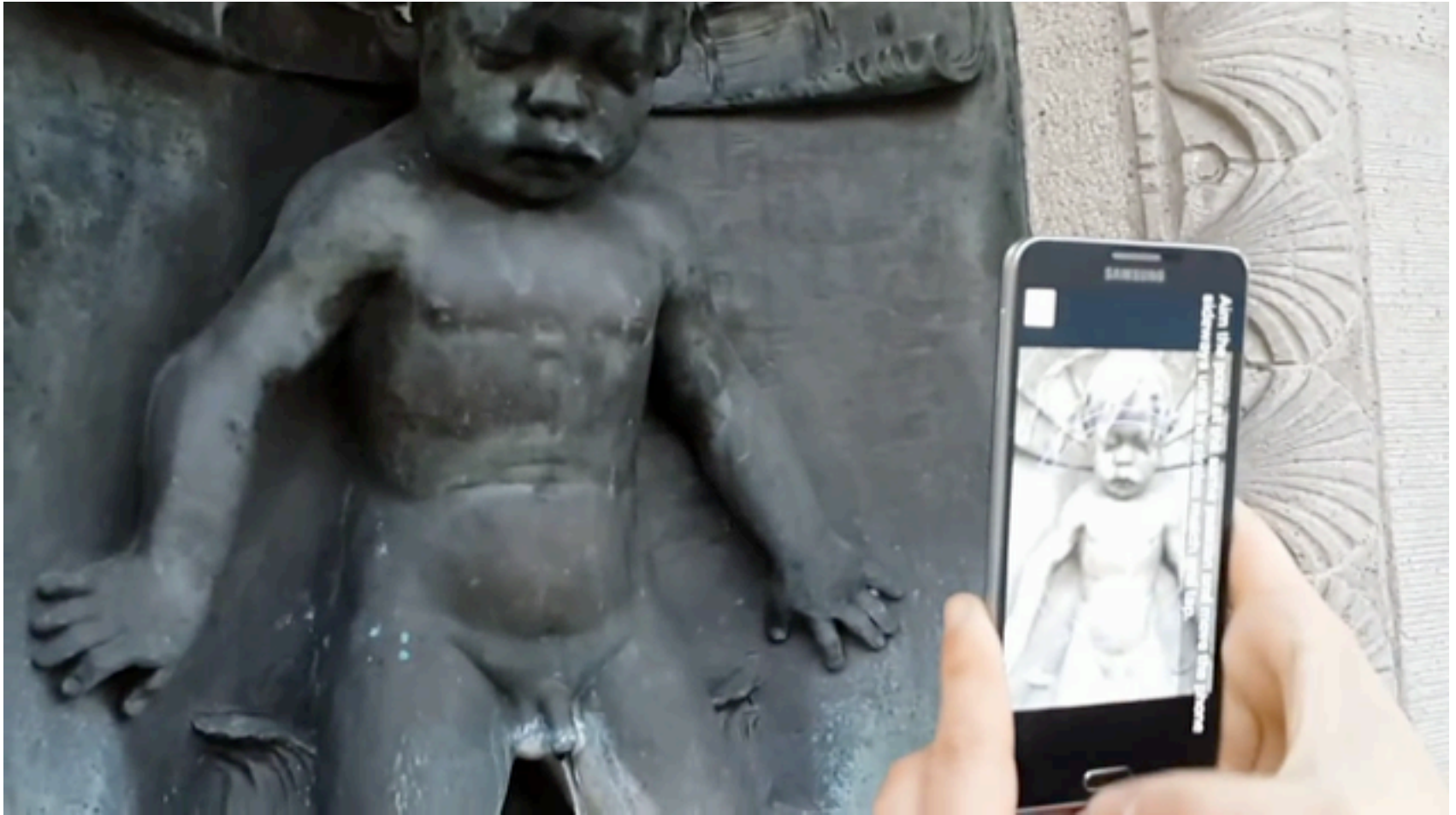
Mobile Visual SLAM + IMU

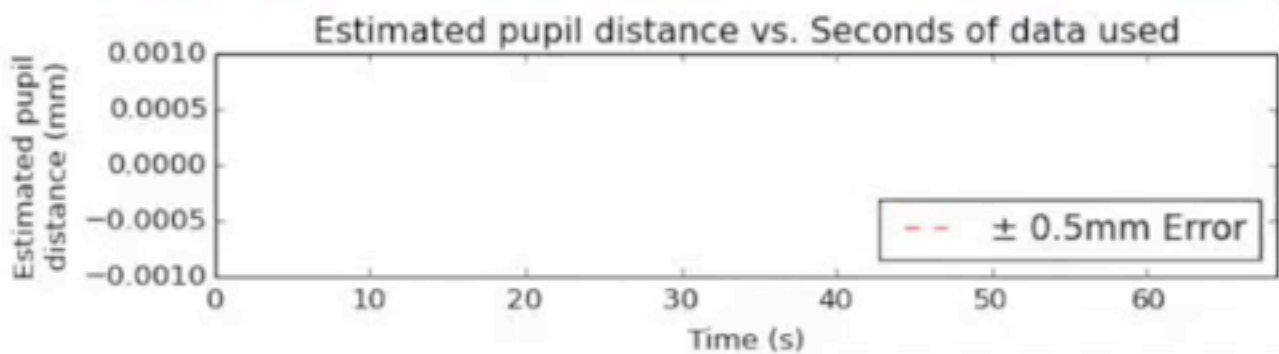
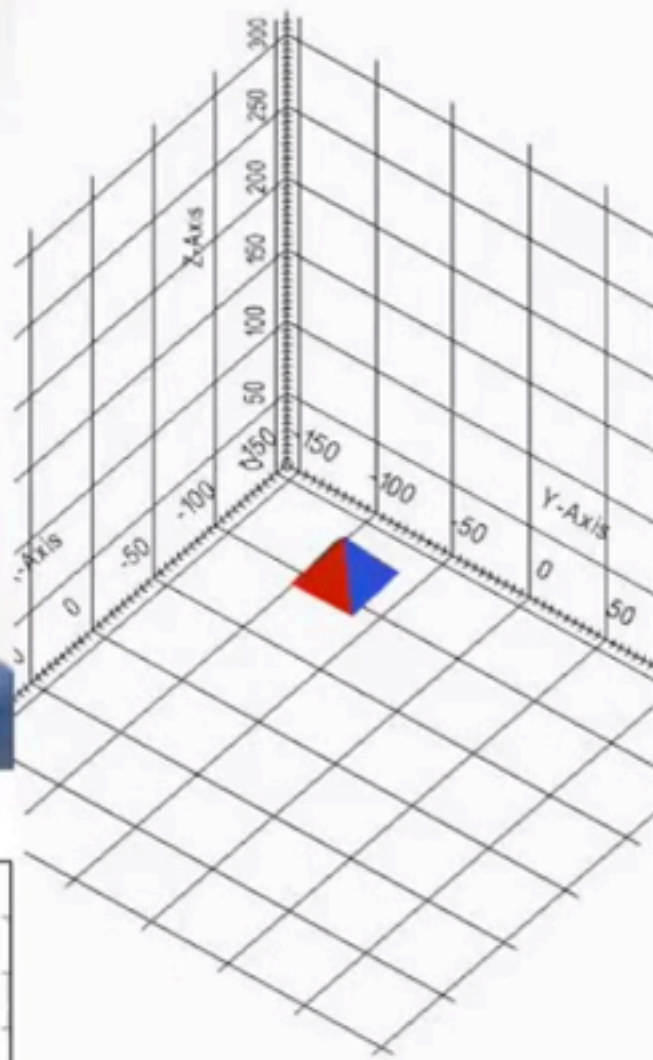
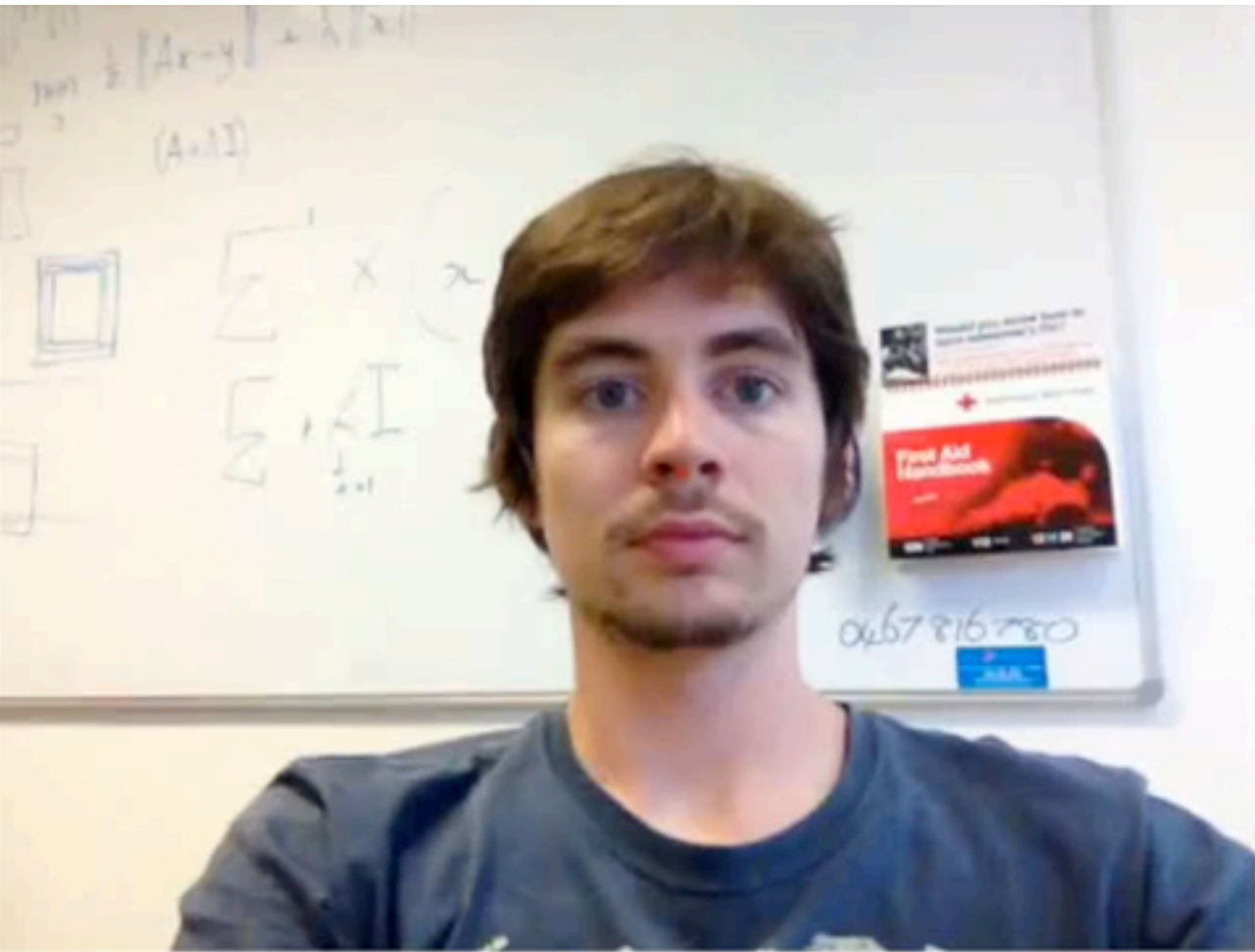


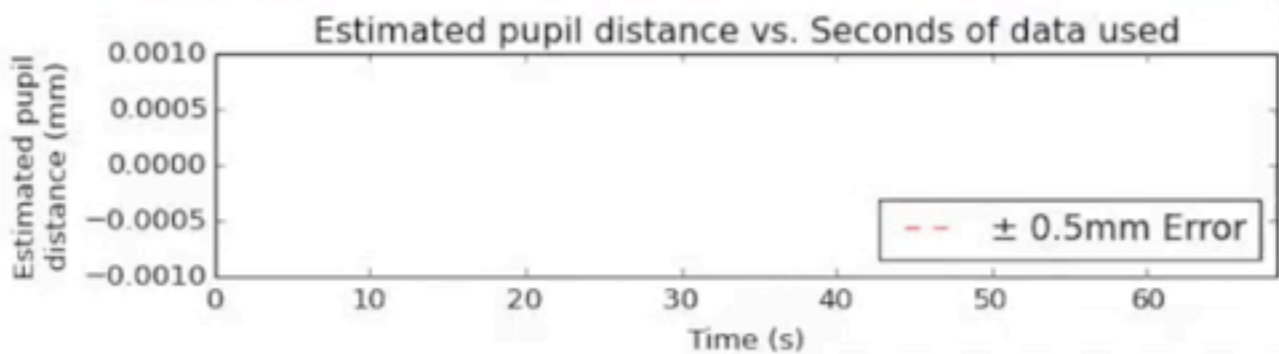
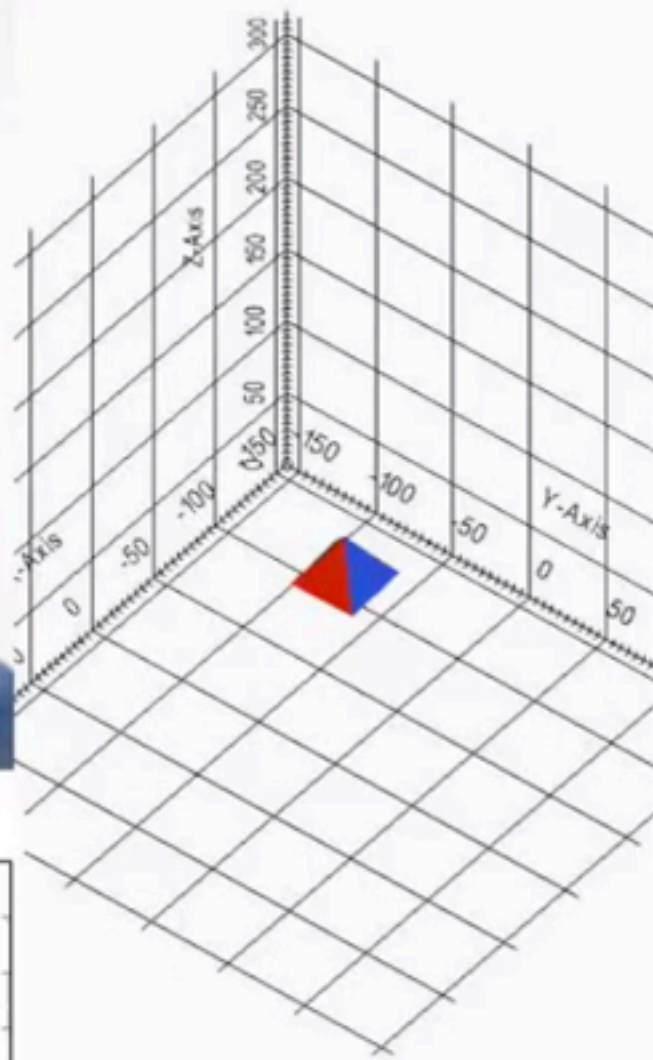
Mobile Visual SLAM + IMU

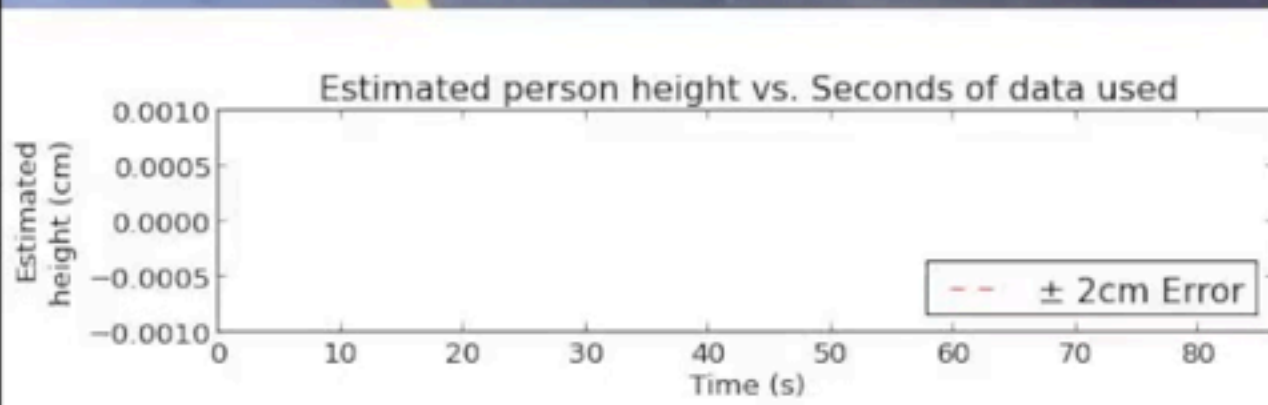
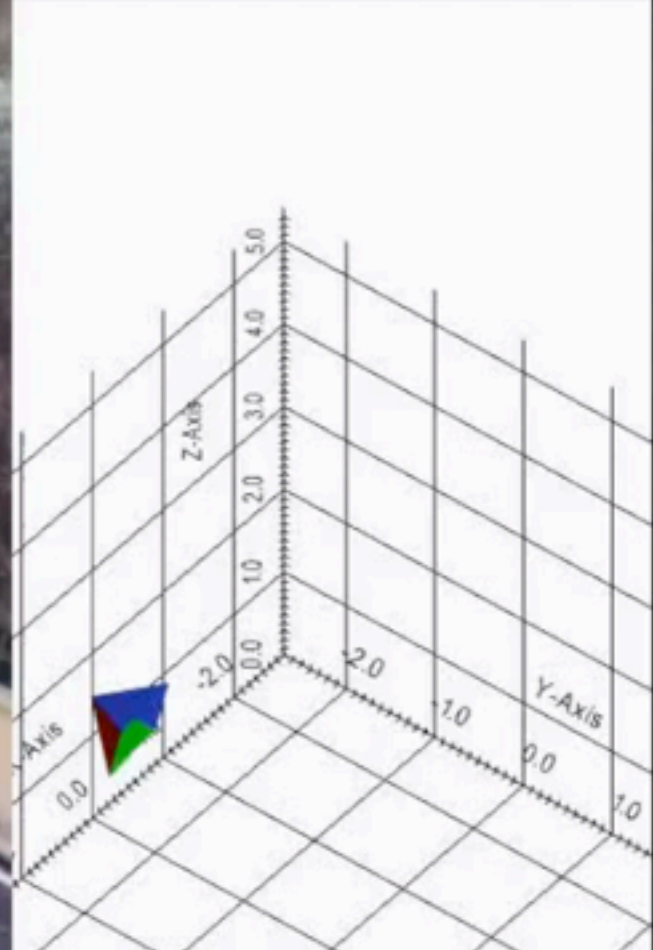


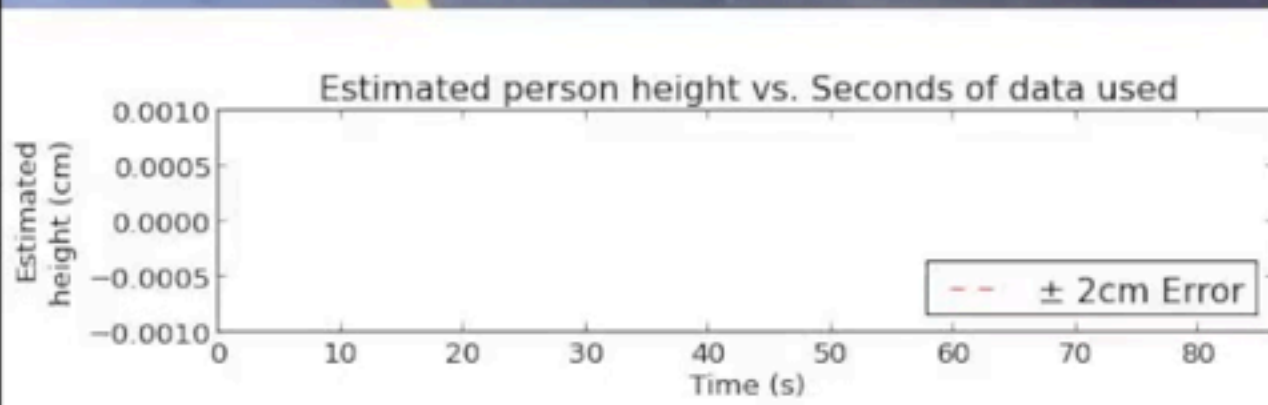
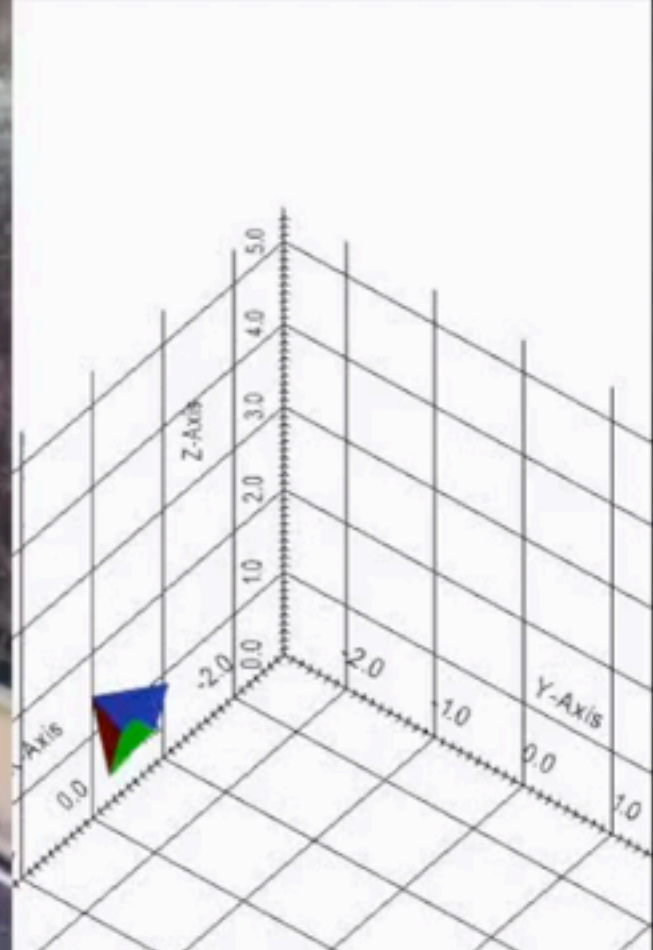
Mobile Visual SLAM + IMU

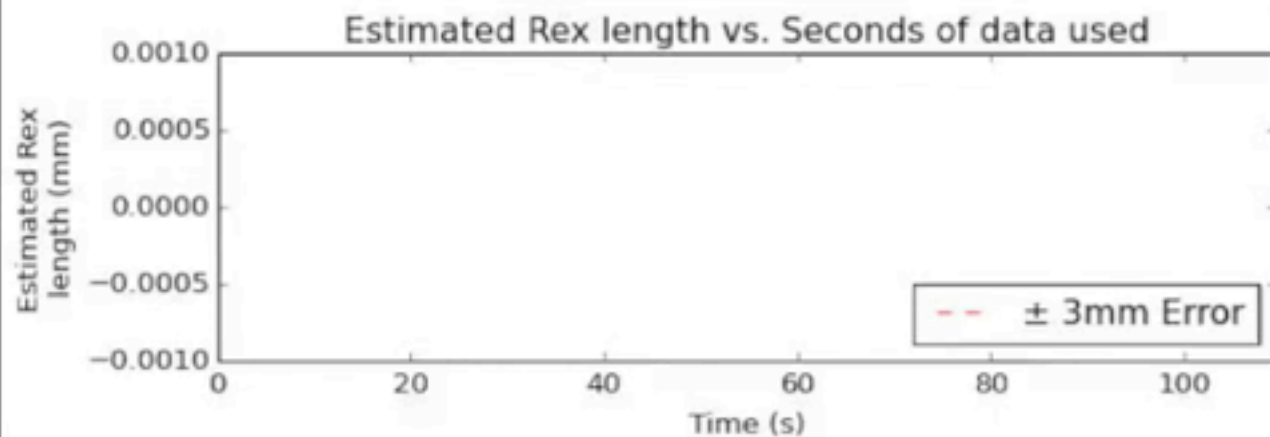
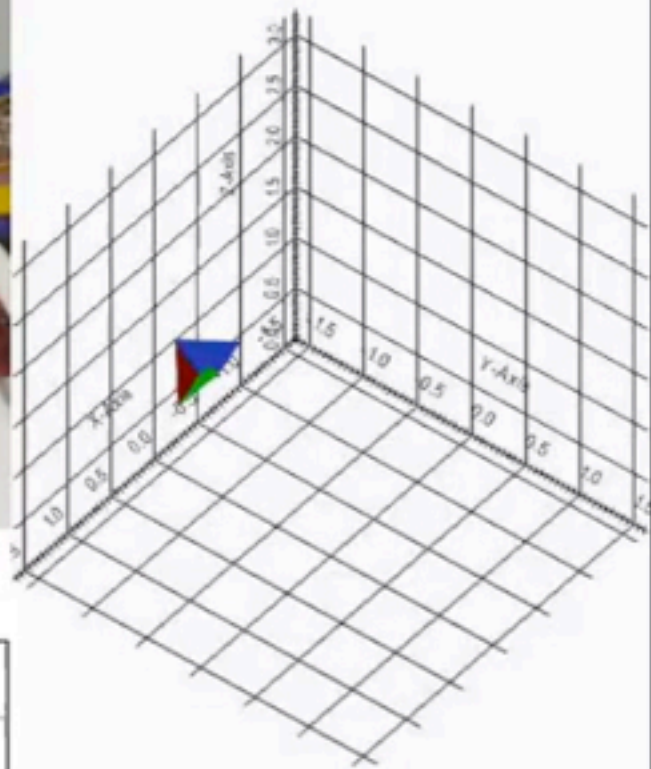
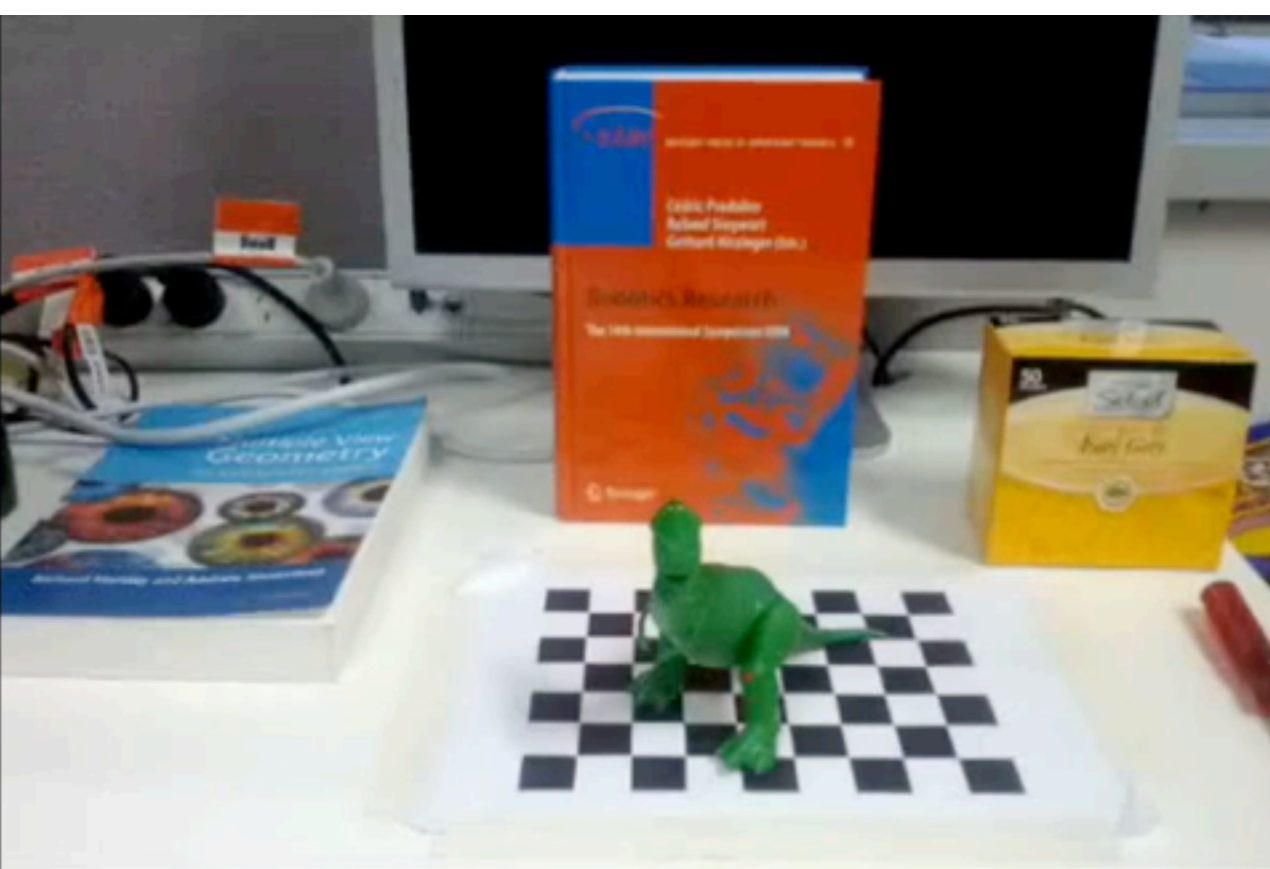




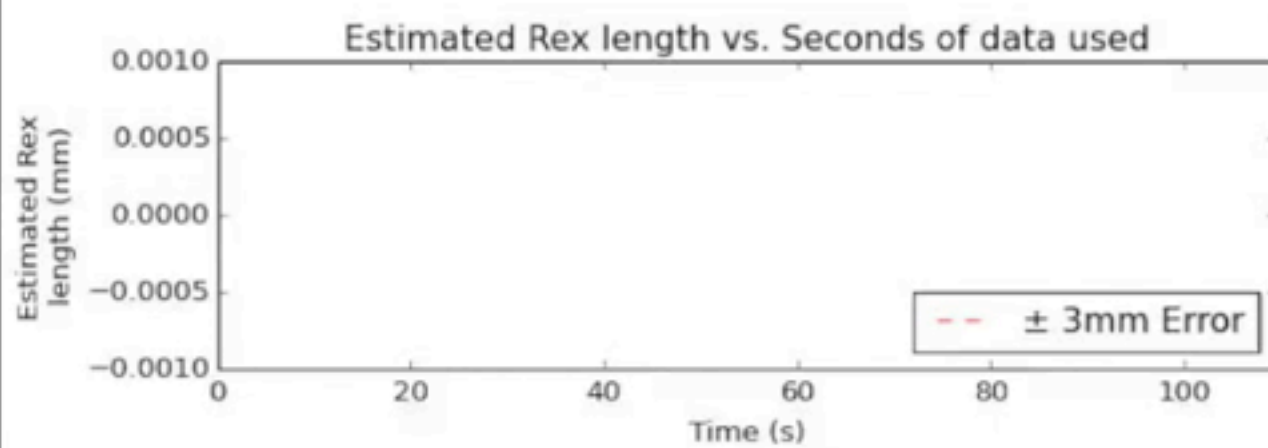
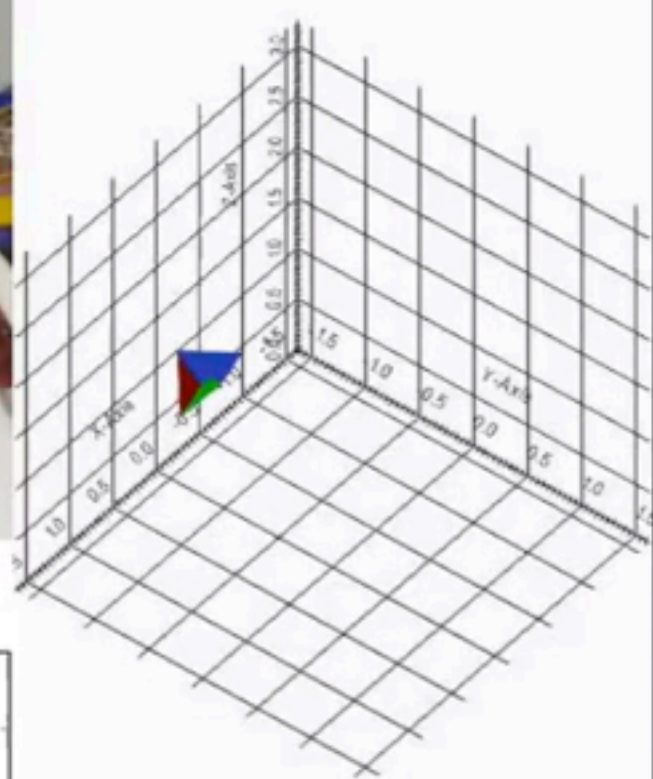
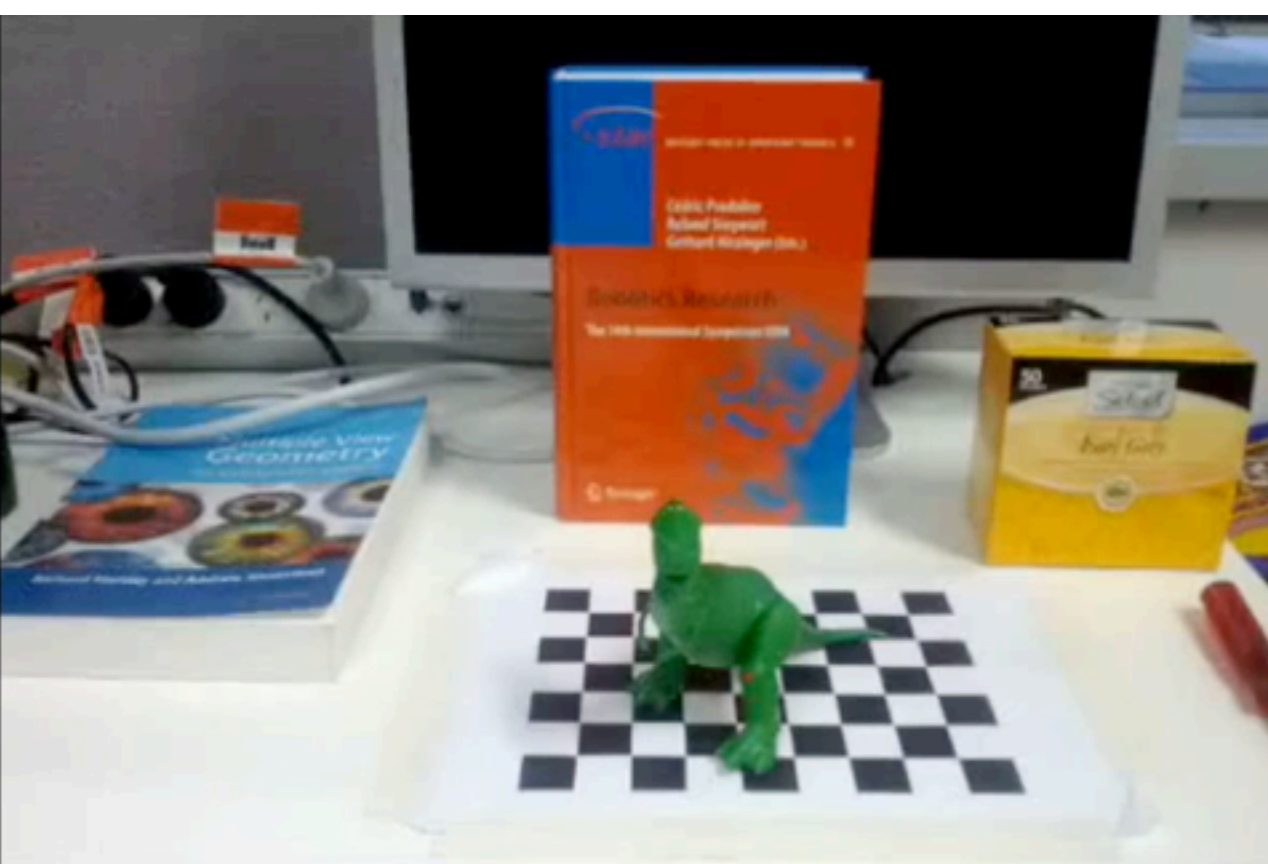








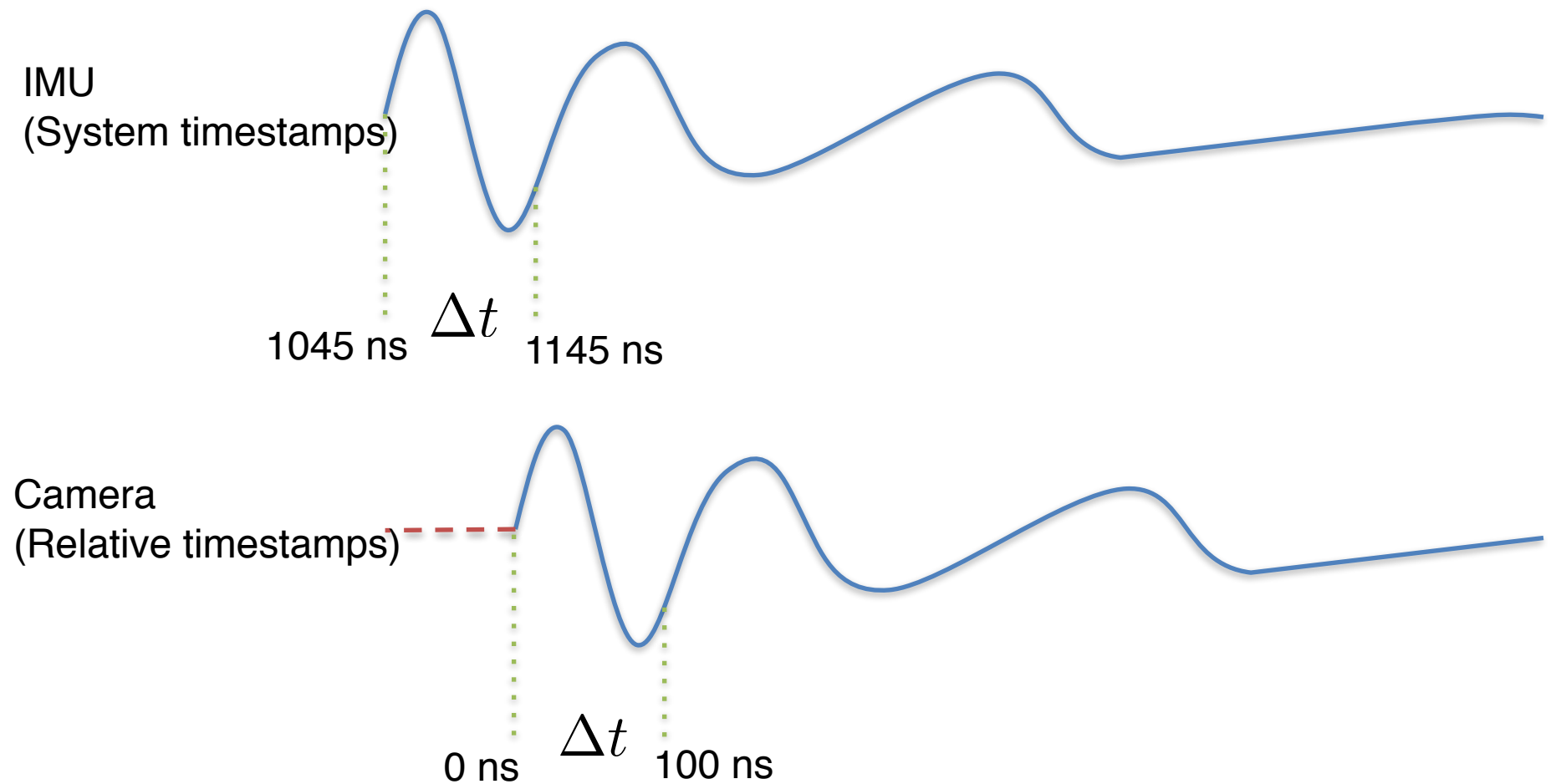
C. Ham, S. Singh, and S. Lucey: Handwaving away scale. (ECCV 2014)



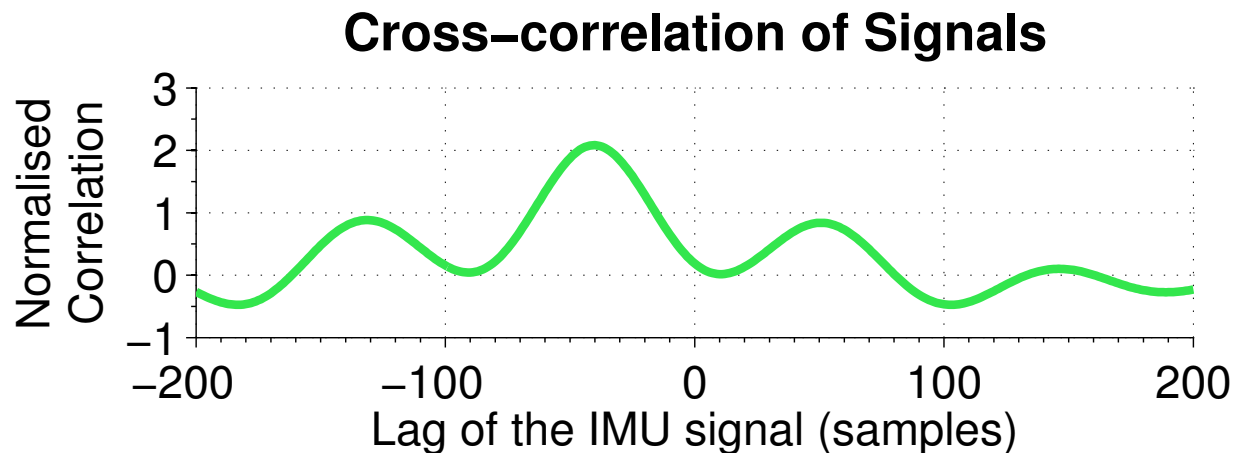
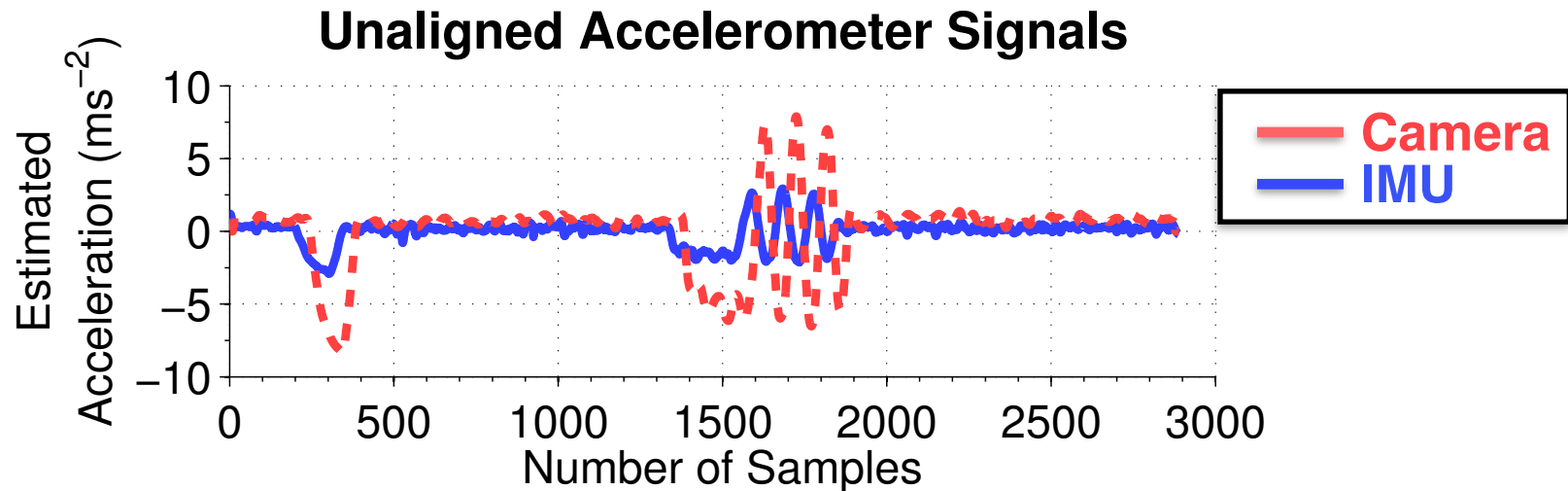
C. Ham, S. Singh, and S. Lucey: Handwaving away scale. (ECCV 2014)

Mobile Platform Issues

- IMU and Camera time stamped differently



Auto-Correlation



More to read...

- Y. Dai, H. Li and L. Kneip “Rolling Shutter Camera Relative Pose: Generalized Epipolar Geometry”, arXiv preprint arXiv:1605.00475 (2016).

